Analysis of the Influence of the Annualized Rate of Rentability on the Unit Value of the Net Assets of the Private Administered Pension Fund NN

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Abstract. Starting from the idea that the profitability of a private pension fund has repercussions on the unit value of the net asset, which is able to directly influence the level of the sums accumulated on the members' account, I consider it useful to know the relation of dependence between the annualized return and unit value of the net asset. To conduct the research, I chose the NN Private Administered Pension Fund, which is part of Romania's Pension Pillar II. With the help of the EViews 9.5 Student / Lite Version software, I aim to obtain a valid econometric model with which I can predict the unit asset value of the net asset according to the evolution of the annualized rate of return. After obtaining a valid model, I will predict the unit asset value of the net asset for two hypothetical levels of the annualized rate of return

Keywords: Pillar II; net asset value, annualized rate of return, econometric model, unifactorial linear regression.

JEL Classification: G23, G28, G29

1. Introduction

The level of pensions to be paid to participants in privately managed pension funds depends on the level of the amounts accrued to the participants' accounts. These are in turn influenced by the amounts with which the participants contribute to the fund, and on the other hand by the return on investments made by the pension funds. If the level of the contribution is closely linked to the gross income of each participant, being specific to each participant in the fund, the return on investment of funds is specific to the fund and influences the level of pensions of all members of the fund. Under these circumstances, I believe it is of interest to analyze the evolution of the unit value of the asset under the influence of the annualized rate of return for a pension fund.

2. Methodology of research

In view of the research conducted in the field of privately managed private pension funds in Romania, we decided to build an econometric model in which to include the actual values of the annualized rates of return for the NN Private Administered Pension Fund and the unit value of the net asset for this fund.

The shape of the model is:

$VUAN = \beta_0 + \beta_1 * RRA$

where: VUAN – the dependent variable, ie the unit value of the net assets of the NN Private Administered Pension Fund recorded on 31 December 2010-2017;

 β_0 – is the free term of the regression line (value for RRA = 0);

 β_1 is the regression coefficient (the amount with which the VUAN changes when the RRA changes with a unit);

RRA – the explanatory variable, represented by the annualized rate of return of the NN Private Administered Pension Fund recorded on 31 December 2010-2017.

For the analysis of the correlations between the two variables of the model, I will use the one-factor linear regression and the annual frequency obtained from the website of the Financial Supervisory Authority (ASF) in Romania.

Using the EViews 9.5 Student / Lite Version software, I will estimate the model using the least squares method and test the validity of the model, the degree of model reliability, the unifactorial regression model assumptions, and the statistical significance of the parameters included in the model.

3. Data used. Defining model variables

Unit Net Asset Value (VUAN) is the pointer used to calculate the amount of money actually available in each participant's personal account.

The annualized rate of return of a privately managed pension fund "is determined by dividing the profitability rate of that fund by 2, measured for the last 24 months preceding the calculation"

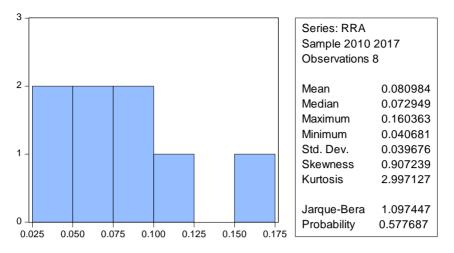
In Fig. 1 are the values recorded on December 31 by the two variables (VUAN and RRA) that are the subject of the analysis. The analyzed period begins with 2010 (one year of which privately managed private pension funds computes and publishes annualized profitability rates) and ends with 2017.

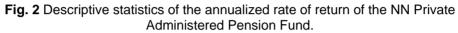
	VUAN	RRA
2010	15.13536	0.160363
2011	15.43008	0.081481
2012	17.01465	0.059391
2013	18.93632	0.102432
2014	20.68960	0.098115
2015	21.53651	0.064416
2016	22.39795	0.040992
2017	23.34290	0.040681

Fig. 1 Evolution of VUAN and RRA during 2010-2017. Source: Author's work based on data available on www.asfromania.ro accessed on 23.06.2018

From the statistical data provided by EViews and presented in Fig. 2 it appears that for the NN Private Administered Pension Fund, the average annualized rate of return for the period between 2010 and 2017 was 8.0984%, with a standard deviation of 0.039676.

The distribution shows positive asymmetry, the higher values being present on the left by the Skewness asymmetry coefficient which has the value of 0.907239 and the coefficient of flattening Kurtosis is 2.997127, very close to 3, which means a normal distribution. Annualized rate of return has evolved between a minimum of 4.0681% recorded in 2017 and a maximum of 16.0363% achieved in 2010, the trend being one of decreasing.





Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

Unit Net Asset Value (VUAN) is the pointer on the basis of which the amount of money accumulated up to a certain point in the individual account of each participant is determined. The profitability of each pension fund is reflected in the value of the VUAN. The annualized rate of return of a pension fund is the main performance indicator of a privately managed pension fund, whose calculation formulas are set by the rules issued by the Romanian Financial Supervisory Authority.

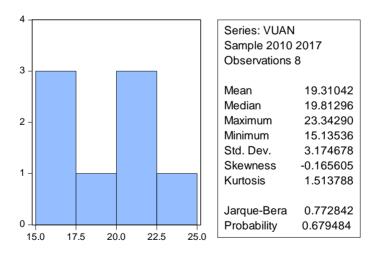
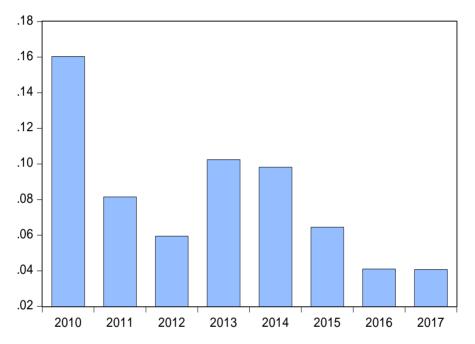


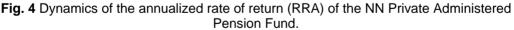
Fig. 3 Descriptive statistics of VUAN for NN Private Administered Pension Fund. Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

Analyzing the statistical data obtained with EViews and presented in Fig. 3 shows that the average VUAN level of the NN Private Administered Pension Fund for the period between 2010 and 2017 was 19.31042 lei, with a standard deviation of 3.174678. The distribution shows a slight negative asymmetry, the higher values being present on the right side, which is evidenced by the coefficient of asymmetry

(Skewness) which has the value of -0.165605 and the coefficient of flattening (Kurtosis) is 1.513788, less than 3, indicating the existence of a platictic distribution. VUAN has increased from a minimum of 15.13536 in 2010 to a maximum of 23.34290 lei reached on December 31, 2017.

The annualized rate of return (RRO) had an annual downward trend except for 2013. This started from the maximum of 16.0363% achieved in 2010 and reached the minimum on 31 December 2017, ie 4.0681%. The average value of the indicator was 8.0984%, which is a rate of return that I consider to be quite good. The annual evolution (reported on 31 December) of the annualized rate of return of the NN Private administered Pension Fund in Pillar II is presented in Fig. 4.





Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

The VUAN Dynamics of the NN Private Administered Pension Fund, as can be seen in Fig. 5, had an upward trend over the period 2010-2017, with years of stronger growth (2011, 2012, 2013 and 2014) and years of moderate growth (2010, 2015, 2016 and 2017)..



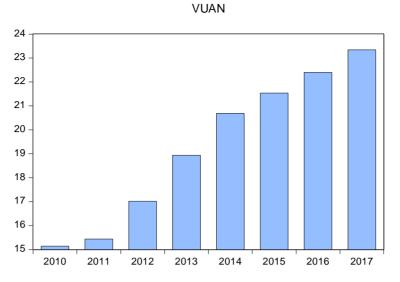


Fig. 5 VUAN Evolution for NN Private Administered Pension Fund. Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

4. Empirical research results

To determine the intensity of the link between the annualized rate of return (RRA) and the unit value of the net asset of the NN Private Administered Pension Fund (VUAN), I will determine the level of correlation between the two variables. The correlation indicates the intensity of the existing link between the two variables included in the econometric model by measuring the degree of scattering of data recorded around the regression line. For this, I will calculate the Pearson correlation coefficient:

$$r_{RRA,VUAN} = \sqrt{R^2} = R = -0,670342,$$

Value obtained from the correlation matrix generated by EViews in Fig. 6

	VUAN	RRA
VUAN	1.000000	-0.670342
RRA	-0.670342	1.000000

Fig. 6 The matrix of correlation of the two variables Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

Next, I will estimate the model parameters. Using the EViews software I will analyze the data series and estimate the regression model parameters by applying the least squares method that generated the results presented in Fig. 7.

Dependent Variable: V Method: Least Square Date: 06/17/18 Time: Sample: 2010 2017 Included observations:	s 08:33			
Variable	Coefficient	Std. Error	t-Statistic	Prob.
C RRA	23.65421 -53.63764	2.159373 24.24000	10.95420 -2.212774	0.0000 0.0689
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood F-statistic Prob(F-statistic)	0.449358 0.357584 2.544531 38.84783 -17.67235 4.896370 0.068880	Mean depen S.D. depend Akaike info c Schwarz cri Hannan-Qui Durbin-Wats	lent var riterion terion nn criter.	19.31042 3.174678 4.918088 4.937948 4.784137 0.973180

Fig. 7 Parameter estimation via MCMMP (Least squares) Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

The model equation is the following:

Demonstrate Variables V/UAN

 $VUAN = \beta_0 + \beta_1 * RRA$ VUAN = 23,65421 - 53,63764 * RRA

The regression coefficient β_1 complements the Pearson correlation coefficient and indicates an indirect link between the variables of the econometric model. At the same time, we can say that an increase with a percentage of the annualized rate of return will attract a VUAN 53.63764 lei decrease. This contradicts the economic theory which indicates that an increase in the annualized rate of return entails an increase in the unit value of the net asset for a privately managed pension fund. Considering this contradiction, we can suspect that the estimated model is not the correct one and we continue the analysis.

The high value of the free term β_0 shows that the influence of factors not specified in the model on VUAN evolution is significant, which leads to the conclusion that the model used can be further deepened to ensure better results.

For the estimated model the link between VUAN and RRA is an indirect and medium intensity. The determination coefficient ($R^2 = R$ -squared = 0,449358) shows that 44.9358% of the VUAN variation is explained by the evolution of the annualized rate of return (RRA), the remainder of the variation can be explained by factors not included in the econometric model. The adjusted determination coefficient (Adjusted R-squared = 0.357584) also takes into account the number of observations included (i = Included observations) and the explanatory variables.

The correlation ratio (R = 0,670342) tends to 1 and shows that the estimated regression model approximates the observation data well, averaging, suggesting that the model can be improved in the future to get better results. The mean square error of estimated errors (S.E. of regression) is 2.544531.

I will continue the analysis by checking the significance of the parameters with

 $-H_0$: $\beta_0 = 0$; $\beta_1 = 0$ (the parameters are not statistically significant, the model is not valid),

 $-H_1$: $\beta_0 \neq 0$; $\beta_1 \neq 0$ (the parameters are statistically significant, the model is valid).

As for the parameter: β_0 : $|t_{calc}| = 10,95420 > 2,4468899 = t_{tab}$, and for the parameter β_1 : $|t_{calc}| = 2,212774 < 2,4468899 = t_{tab}$ the econometric model is retained and the analysis continues. In practice, for a 5% significance threshold, if the statistical t values are greater than or equal to 2, the alternative assumption is accepted, which implies that the parameters are statistically significant and the model is valid. This is not supported by the probability associated with the parameter β_1 (6.89%) which is higher than the materiality threshold (5%).

To test the validity of the model we have the following assumptions:

- H_0 : the model is not statistically valid (MSR=MSE)

- H_1 : the model is statistically valid (MSR>MSE)

We can assert that the model is not statistically significant following the F (F = 4.96370 $< F_{critic} = 6.60789097$) test, so I will accept the null hypothesis (H₀) and reject the alternative hypothesis (H_1) , the model not being valid for a significance level prob. (F-statistic) = 0.0688080, greater than 5%.

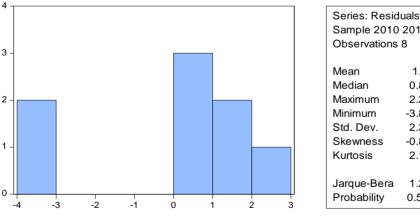
The functional form is linear:

5. The normality of distribution of random errors and their average

To test the normality hypothesis of random errors I will use the Jarque-Bera test with the following assumptions:

- H_0 : random errors have normal distribution;

- H_1 : random errors do not have normal distribution.



Sample 2010 2017 Observations 8				
Mean	1.13e-14			
Median	0.859393			
Maximum	2.298053			
Minimum -3.853678				
Std. Dev. 2.355778				
Skewness -0.888427				
Kurtosis 2.159396				
Jarque-Bera 1.287942				
Probability 0.525203				

Fig.8 The Jarche-Bera Test

Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

The probability associated with this test is 0.525203 that tends to 1, so I will accept the null hypothesis (H_0) , random errors with normal distribution. It can be seen To observe whether the random errors are homoscedastic or not, I will apply the White test with assumptions:

-*H*₀: there is homoscedasticity;

-*H*₁: there is heteroscedasticity.

Heteroskedasticity Test: White

F-statistic	0.760375	Prob. F(2.5)	0.5149
Obs*R-squared	1.865735	Prob. Chi-Square(2)	0.3934
Scaled explained SS	0.608379	Prob. Chi-Square(2)	0.7377

Test Equation: Dependent Variable: RESID² Method: Least Squares Date: 06/17/18 Time: 08:35 Sample: 2010 2017 Included observations: 8

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C RRA⁄2 RRA	-4.361618 -1493.227 260.1448	11.91048 1371.960 274.0197	-0.366200 -1.088390 0.949365	0.7292 0.3261 0.3860
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood F-statistic Prob(F-statistic)	0.233217 -0.073496 5.791472 167.7057 -23.52259 0.760375 0.514851	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion Hannan-Quinn criter. Durbin-Watson stat		4.855979 5.589702 6.630646 6.660437 6.429721 1.405370

Fig. 9 The White Test

Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

After applying the test, we obtain that Prob. (F-statistic) for calculated statistics is greater than 5% and 0.5149 respectively, so there is a high probability of error by rejecting the null hypothesis, so we accept the null hypothesis (H_0) that random errors are homoscedastic.

Critical values of the Durbin-Watson statistic for a significance threshold of 5% obtained from the statistical tables are dL = 1.08 and dU = 1.36.

Since the Durbin-Watson statistic = 0.973180, provided by EViews in Fig. 7, is in the range 0 <0.973180 <1.08, it indicates the existence of positive first order autocorrelation.

I will correct the first order autocorrelation by differentiating the regressors, and the result provided by EViews is shown in Fig. 10.

Dependent Variable: D(VUAN) Method: Least Squares Date: 06/18/18 Time: 00:21 Sample (adjusted): 2011 2017 Included observations: 7 after adjustments

Variable	Coefficient	Std. Error	t-Statistic	Prob.
D(RRA) C	13.16434 1.397582	4.034468 0.154503	3.262967 9.045682	0.0224
R-squared Adjusted R-squared	0.680449 0.616539	Mean dependent var S.D. dependent var		1.172505 0.590680
S.E. of regression Sum squared resid	0.365774 0.668954 -1.714742	Akaike info criterion Schwarz criterion		1.061355 1.045901 0.870343
Log likelihood F-statistic Prob(F-statistic)	-1.714742 10.64695 0.022372	Hannan-Quinn criter. Durbin-Watson stat		0.870343 1.651934

Fig. 10 Unifactorial regression after correcting self-correction of errors. Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

The equation of the adjusted pattern is the following:

$$D(VUAN) = \beta_0 + \beta_1 * D(RRA)$$

where: D(VUAN)=VUAN - VUAN(-1) and D(RRA)=RRA - RRA(-1) D(VUAN) = 1,397582 + 13,16434 * D(RRA)

The regression coefficient β_1 indicates a direct link between the econometric model variables. At the same time, we can say that an increase with a percentage of D (RRA) will attract an increase of 13.16434 lei for D (VUAN).

The low value of the free term β_0 indicates that the influence of factors not specified in the model on the D (VUAN) evolution is not significant, which leads to the conclusion that the model is correctly specified.

The relationship between D (UAN) and D (RRA) is a direct one and a medium intensity.

The determination coefficient (R^2 = R-squared = 0.680449) shows that 68.0449% of the variance D(VUAN) is explained by D(RRA) evolution, the remainder being explained by factors which are not included in the econometric model. The adjusted determination coefficient (Adjusted R Squared = 0.616539) also takes into account the number of observations included (i = Included observations) and the explanatory variables.

t:

 $-H_0$: $\beta_0 = 0$; $\beta_1 = 0$ (the parameters are not statistically significant, the model is not valid)

I will continue the analysis by checking the significance of the parameters with

 $-H_1: \beta_0 \neq 0$; $\beta_1 \neq 0$ (the parameters are statistically significant, the model is valid)

 $\begin{array}{l} -\beta_0: \; |t_{calc}| = 9.045682 > 2.4468899 = t_{tab}, \\ -\beta_1: \; |t_{calc}| = 3.262967 > 2.4468899 = t_{tab} \end{array}$

We note that both parameters are larger than the tabulated value, which allows us to reject the null hypothesis and accept the alternative hypothesis that the parameters are statistically significant, the model is valid.

This is also confirmed by the probabilities associated with the two parameters (2.24% and 0.03%) that are greater than the significance threshold of 5%.

To test the validity of the model we have the assumptions

-H₀: the model is not statistically valid (MSR=MSE)

- H_1 : the model is statistically valid (MSR>MSE)

We can say that the model is statistically significant following the F test (F-statistic = 10.64695> F_{critic} = 6,60789097), so I will reject the null hypothesis (H_0) and accept the alternative hypothesis (H_1), the model being valid for a probability significance level Prob. (F-statistic) = 0.022372, less than the significance threshold of 5%.

The functional form is linear:

D(VUAN) = 1,397582 + 13,16434 * D(RRA)

To test the normality hypothesis of random errors I will use the Jarque-Bera test with the following assumptions:

-H₀: random errors have normal distribution;

- H_1 : random errors do not have normal distribution.

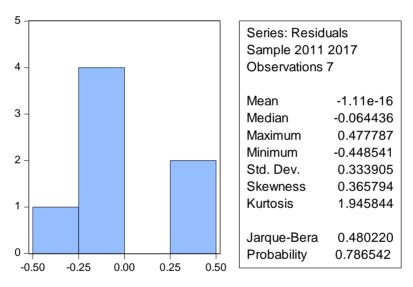


Fig. 11 The Jarche-Bera Test

Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

The probability associated with this test is 0.786542 which tends to 1, so I will accept the null hypothesis (H_0), random errors with normal distribution. It can be seen from Fig. 11 that the average random error is -1,11e-16 = -1.11/100000000000000000, being very close to zero.

To see if random errors are homoscedastic or not, I will apply the White test with the following assumptions::

-*H*₀: there is homoscedasticity;

-H₁: there is heteroscedasticity.

Heteroskedasticity Test: White

F-statistic Obs*R-squared Scaled explained SS	1.480397 2.977470 0.718424	Prob. F(2,4) Prob. Chi-So Prob. Chi-So	0.3302 0.2257 0.6982		
Test Equation: Dependent Variable: RESID ² Method: Least Squares Date: 06/21/18 Time: 21:43 Sample: 2011 2017 Included observations: 7					
Variable	Coefficient	Std. Error	t-Statistic	Prob.	
C D(RRA)⁄2 D(RRA)	0.134186 -36.37138 -0.860912	0.043517 21.87620 1.297686	3.083544 -1.662600 -0.663421	0.0368 0.1717 0.5433	
R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood F-statistic Prob(F-statistic)	0.425353 0.138029 0.093202 0.034747 8.636954 1.480397 0.330219	Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion Hannan-Quinn criter. Durbin-Watson stat		0.095565 0.100388 -1.610558 -1.633740 -1.897076 1.901348	

Fig. 12 The White Test

Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

Let's get that Prob. F statistics calculated is greater than 5% respectively 0.3302 = 33.02%, so there is a high probability of rejecting the null hypothesis wrong, so we accept the null hypothesis (H_0) that are homoscedastic random errors.

Critical values of the Durbin-Watson statistic for a significance threshold of 5% obtained from the statistical tables are dL = 1.08 and dU = 1.36.

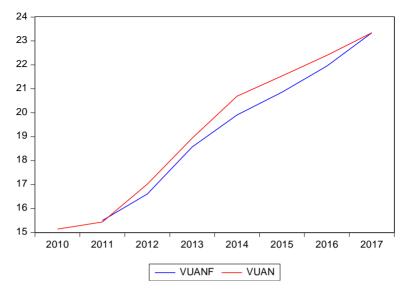
The Durbin-Watson statistic = 1.651934, provided by EViews in Fig.10, is in the range 1.36> 1.651934> 2.72, which indicate us the inexistence of an autocorrelation.

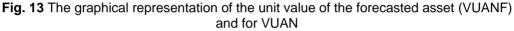
After elimination of the autocorrelation of the residues, the obtained model is statistically significant, with an average credit, the exogenous variable is statistically significant as the constant.

It fulfills all the assumptions of the classic simple regression model, and still has an average credit rating (R^2 = R-squared = 0.680449), approximating the observation data well. All parameters of the final model are statistically significant with Prob. associated less than 5%.

The determinant coefficient (R-squared = 0.680449) shows that 68.0449% of the variance of the dependent variable is explained by the RRA variation.

In order to assess whether the linear regression model is satisfactory and is good for predicting, I will represent in Fig. 13 both the projected values of the unit value of the net asset (VUANF) and the real values of the VUAN.







The chart shows that the predicted value does not deviate significantly from the real value, indicating an econometric model that can be used successfully to make forecasts.

I will then predict the VUAN level for the end of 2018, given that the RRA will be: 4% and 5%, respectively.

At this stage of econometric modeling, I will predict VUAN of the privately managed pension fund for December 31, 2018, given that the RRA will have the value of A: 4% and B: 5%. The two forecasts are represented in Fig.14 and Fig. 15.

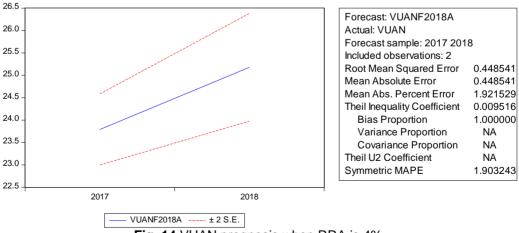


Fig. 14 VUAN prognosis when RRA is 4%.

Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

The EViews forecast shows that VUAN will have the level of 25.18 lei at 31 December 2018. At the same time it can be guaranteed with a 95% probability that the VUAN level at 31 December 2018 will be in the range of [23.98; 26.38].

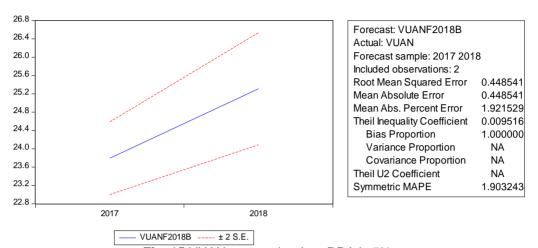
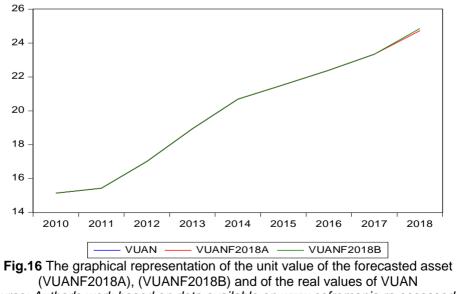


Fig. 15 VUAN prognosis when RRA is 5%. Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

The forecast with EViews shows that VUAN will have the level of 25.31 lei at 31 December 2018. At the same time it can be guaranteed with a 95% probability that the VUAN level at 31 December 2018 will fall within the range of [24.09; 26.54].

To illustrate the results obtained in the two cases I will represent graphically alongside the real evolution of VUAN and the two forecasts in Fig. 16.



Source: Author's work based on data available on www.asfromania.ro accessed on June 23, 2018 using EViews 9.5 Student / Lite Version.

The results obtained in the two forecasts highlight the growth trends of the VUAN indicator in the two annualized rate of increase of the annualized rate of return

to 4% and 5%. This is in line with the theory that increasing the annualized rate of return leads to an increase in the net asset value of the net asset if the other factors of influence remain unchanged.

If we report the VUAN projected for December 31, 2018, in the conditions of increasing the rate of return to 4% (VUANF2018A), at the VUAN forecast for the same date, given at the 5% annualized rate of return (VUANF2018B), will note that between the two levels we have a difference of 0.13 lei, which means that a 1% increase in the annualized rate of return entails an increase of approximately 13 bani of the unit value of the net asset.

6. Conclusions

As a result of the data processing using the one-factor linear regression, we obtained an econometric model with an average creditworthiness that captures the way in which the annualized rate of return dynamics influences the evolution of the unit value of the net assets of the NN Private Administered Pension Fund.

The unifactorial model obtained by estimation is:

D(VUAN) = 1,397582 + 13,16434 * D(RRA)

The EViews program estimated the above model and obtained the following final results:

-the determination coefficient confirms that the annualized rate of return rate influences the increase of the unit value of the net asset in the case of the NN Private Administered Pension Fund in the amount of 68.0449%.

- there is a significant direct relationship between the net asset value and the annualized rate of return. It can be said that an increase by one percent of the annualized rate of return will result in an increase of 0.13 monetary units of the VUAN.

I appreciate that the model is good to make predictions with it, but can be improved by adding other explanatory variables and converting it into a multifactorial regression model with a higher level of determination coefficient (R-squared = 0.680449).

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